X(6th Sm.)-Physics-H/[DSE-B2]/CBCS

2022

PHYSICS — HONOURS

Paper : DSE-B2

[(a) Communication Electronics]

Full Marks : 65

The figures in the margin indicate full marks.

Candidates are required to give their answers in their own words as far as practicable.

Group - A

1. Answer any five questions :

- (a) In an FM system, the frequency deviation is about 20.5 kHz and a modulating signal frequency is 5 kHz. Determine the modulation index and carrier swing.
- (b) Assume the message signal $x(t) = 15 \cos (2\pi t)$ volts and carrier wave $c(t) = 45 \cos (100\pi t)$ volts. Derive AM wave for 30% modulation.
- (c) What is sampling? State sampling theorem.
- (d) What is multiplexing? Name the types of multiplexing.
- (e) What is demodulation?
- (f) Explain the following terms in connection with satellite communication :
 - (i) geostationary satellite,
 - (ii) uplink and downlink frequencies.
- (g) What are SIM and IMEI number in mobile communication?

Group - B

2. Answer any three questions :

- (a) (i) Show that the total power of a fully amplitude modulated wave is 1.5 times the unmodulated carrier power.
 - (ii) Show that the AM wave can be represented by a carrier and two side bands. 3+2
- (b) How can you design an amplitude modulator by using an amplifier whose input v_i and output (v_0) characteristics is $v_0 = a_1v_i + a_2v_i^2$? where a_1 and a_2 are constants.
- (c) (i) How is digital modulation different from analog modulation?
 - (ii) Describe amplitude shift keying (ASK).
 - (iii) Define bit rate.

Please Turn Over

2×5

2+2+1

(2)

- (d) (i) Find the Nyquist rate for the signal $x(t) = 25 \cos (500\pi t)$.
 - (ii) Find the bandwidth of 8-PSK.
 - (iii) The upper and lower cut-off frequencies of a resonant circuit are found to be 8.07 MHz and 7.93 MHz respectively. Calculate the bandwidth.
- (e) What do you mean by transponder in satellite communication? What are their basic components? 3+2

Group - C

Answer any four questions.

- 3. An audio signal : $15 \sin 2\pi (1500t)$
 - Amplitude modulates a carrier : $60 \sin 2\pi (100000t)$.
 - (a) Sketch the audio signal.
 - (b) Sketch the carrier.
 - (c) Construct the modulated wave.
 - (d) Determine the modulation factor and percentage modulation.
 - (e) What are the frequencies of the audio signal and carrier?
 - (f) What frequencies would show up in a spectrum analysis of the modulated wave? 1+1+2+2+2+2
- 4. (a) Find the expression of frequency modulated (FM) wave.
 - (b) A 80 MHz carrier is frequency modulated, the modulation index being 4. The frequency of information signal is 10 kHz. What is the maximum frequency deviation?
 - (c) What do you mean by resistor noise? Calculate the thermal noise voltage developed in a resistor $R = 100 \Omega$. The bandwidth of the circuit is 5 kHz at room temperature 30°C. (Given $k_B = 1.38 \times 10^{-23} \text{ J/K}$) 3+3+(2+2)
- 5. (a) Draw the circuit diagram for generation of PAM signal and explain its operation.
 - (b) Draw the block diagram of PAM signal reception.
 - (c) Draw the circuit diagram of a zero order holding circuit. (3+3)+2+2
- 6. (a) Define μ -law for companding. Define unipolar RZ and NRZ.
 - (b) What is constellation diagram? Draw the diagram for 8-PSK.
 - (c) How can non-uniform quantization be used to increase SNR?
- 7. (a) What is path loss of satellite communication system? How is the path loss related to the gain and power of the transmitting and receiving antenna?
 - (b) In satellite communication $P_t = 23 \ dB_m$, $G_t = 2dB_i$, $G_r = 2dB_i$, $P_r = -71 \ dB_m$. Find the path loss. Where P_t = Power of a transmitter, G_t = Gain of a transmitter, P_r = Power of a receiver, G_t = Gain of a receives.
 - (c) Draw the block diagram of Earth station.
- 8. (a) What is Carson's rule of thumb for the determination of bandwidth in FM station?
 - (b) Describe the basic principle of satellite communication.
 - (c) What are the differences among 2G, 3G and 4G technologies in mobile communication system?

3+4+3

(2+3)+3+2

(2+2)+(2+2)+2

Paper : DSE-B-2

[(b) Advanced Statistical Mechanics]

Full Marks : 65

The figures in the margin indicate full marks. Candidates are required to give their answers in their own words as far as practicable.

Group – A

1. Answer any five questions :

- (a) Explain the following statement 'Negative temperatures are hotter than positive temperatures'.
- (b) A three-level single particle system has five microstates with energy 0, ε , ε , ε , and 2ε . What will be the mean energy of the system if it is in equilibrium with a heat bath at temperature T?
- (c) Give a schematic diagram of chemical potential (μ) vs. temperature (T) curves for two different systems the ideal Bose gas and the ideal Fermi gas.
- (d) Three identical spin 1/2 particles of mass *m* are free to move within a one-dimensional rigid box of length *L*. Assuming that they are non-interacting, find the energies of the two lowest energy

eigenstates in units of
$$\frac{\pi^2 \hbar^2}{2mL^2}$$

- (e) In a thermodynamic system in equilibrium, each particle can exist in three possible states with probabilities 1/2, 1/3, and 1/6 respectively. Find the per particle entropy of the system.
- (f) What is 'Chandrasekhar mass limit'?
- (g) Draw the specific heat curve for a Bose gas as a function of temperature (T) on both sides of critical temperature (T_c) .

Group - B

- 2. Answer any three questions :
 - (a) Consider a classical gas of N identical indistinguishable particles in a two-dimensional square box of side L. If the total energy of the gas is E, find the number of accessible microstates and the entropy.
 - (b) Calculate the pressure exerted by an ideal Fermi gas at 0 K. What is the physical reason for the non-zero pressure at absolute zero?
 - (c) The wave function $\psi(t)$ of an isolated system is given by $\psi = \sum_n a_n(t)\varphi_n$ where $\{\varphi_n\}$ is the complete orthonormal set of stationary wave functions. Write down the postulate of equal a priori probabilities and the random phases in terms of a_n .

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5×3

2×5

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(d) A particle hops on a one-dimensional lattice with lattice spacing a. The probability of the particle to the neighbouring site to its right is p, while the corresponding probability to hop to the left is

q = 1-p. Find the root-mean-squared deviation $\Delta x = \sqrt{\langle x^2 \rangle - \langle x \rangle^2}$ in displacement after N steps.

(e) Use canonical ensemble to prove that specific heat (C_v) at thermal equilibrium cannot be negative.

Group - C

Answer any four questions.

- (a) Show that the relative root-mean-squared fluctuation in energy of an N-particle system in contact with a heat reservoir varies as 1/√N. Hence comment on the equivalence of the canonical ensemble to the microcanonical ensemble in thermodynamic limit.
 - (b) An ideal collection of N two-level systems is in thermal equilibrium at temperature T. Each system has a ground state energy $-\varepsilon$ and an excited state energy $+\varepsilon$. Prove that the Helmholtz free energy

of the system is
$$A = -Nk_BT \ln\left\{2\cosh\left(\frac{\varepsilon}{k_BT}\right)\right\}.$$
 (5+2)+3

4. (a) Write down the grand partition function of an ideal Bose gas of fugacity z, volume V and temperature T.

(b) The number of Bosons in the excited states can be expressed as $N_e = N - N_0 = \frac{V}{\lambda^3} g_{\frac{3}{2}}(z)$, where

 $\lambda = h/\sqrt{2\pi m k_B T}$ and $g_{\frac{3}{2}}(z)$ is the monotonically increasing Bose function. Given that the largest value (≈ 2.612) of $g_{\frac{3}{2}}(z)$ is bounded at z = 1, derive the condition to obtain Bose-Einstein condensate.

- (c) Show that in the condensed phase $(T < T_C)$, $N = N_0 + N \left(\frac{T}{T_C}\right)^{3/2}$. 2+5+3
- 5. Consider the ionization of atomic hydrogen into a hydrogen ion and an electron : $H \Rightarrow H^+ + e^-$. The number densities of the neutral hydrogen atoms, the hydrogen ions and the electrons at temperature T are n_H , n_H^+ , and n_e respectively.
 - (a) Ignoring the excited bound states derive the Saha ionisation equation

$$\frac{n_H + n_e}{n_H} = \frac{g_H + g_e}{g_H} \frac{\lambda_H^3}{\lambda_{H^+}^3 \lambda_e^3} e^{-\frac{1}{k_B T}}$$

where the gs represent the statistical weights of the three species — the neutral hydrogen atoms, the hydrogen ions and the electrons. The λ s represent their thermal wavelengths $\left(\lambda = h/\sqrt{2\pi m k_B T}\right)$ and I is the ionization energy of a hydrogen atom.

(4)

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(b) Since, $g_H = g_e = 2$, $g_{H^+} = 1$, $m_{H^+} \approx m_H$ and $n_H = n_e$ (overall charge neutrality) show that we may

write Saha's equation as
$$\frac{x^2}{1-x} = \frac{1}{n_e \lambda_e^3} e^{-\frac{1}{k_B T}}$$
, where $x = \frac{n_{H^+}}{\left(n_H + n_{H^+}\right)}$ is the fraction of hydrogen

atoms that are ionised.

- (c) At the surface of the sun the temperature is about 5800 K and the number density of electrons is $2 \times 10^{19} m^{-3}$. Using the Saha's equation in (b) show that less than one hydrogen atom in 10000 is ionised. 5+3+2
- 6. (a) The energy eigenvalues of a one-dimensional harmonic oscillator are given by

$$E_n = \left(n + \frac{1}{2}\right) \hbar \omega, n = 0, 1, 2, \dots$$

Find the internal energy of a system of N such independent harmonic oscillators in thermal equilibrium at temperature T. Calculate $C_{P}-C_{V}$ for this system.

(b) The Hamiltonian of a classical oscillator in two-dimension in plane polar coordinate is

$$H = \frac{p_r^2}{2m} + \frac{p_{\theta}^2}{2mr^2} + \frac{1}{2}kr^2$$

where the symbols have their usual meaning. Calculate < H >. You may use the generalised equipartition theorem. (4+2)+4

7. (a) Consider the Hamiltonian for the Ising model with N spins

$$H = -J\sum_{\langle ij\rangle} s_i s_j$$

with $s_i = \pm 1$, J > 0 and $\sum_{\langle ij \rangle}$ is a sum over nearest neighbours. Within Bragg Williams approximation

the average magnetization per spin (m) can be expressed by the following relation :

$$m = \tanh(J\gamma m/k_{\rm B}T),$$

where γ is the number of nearest neighbours. Use this relation to show that there exists a critical temperature $T_C = J\gamma/k_B$ below which the system can have a non-zero spontaneous magnetization and above cannot.

(b) Calculate the entropy $S = -k_B T_r(\rho l n \rho)$ for the following density matrix $\rho = \begin{bmatrix} \tau - 1 & 0 \\ 0 & \tau + 1 \end{bmatrix}$, where τ

is a real parameter and the rest of the symbols have usual meaning.

(c) For a system having $V^{\frac{2}{3}}E$ = constant, calculate the pressure, *P* as a function of energy, *E* and volume, *V*. Hence find the relation between *P*, *V* and *E*. 4+3+3

Please Turn Over

(5)

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- 8. (a) Consider the degeneracy parameter $e^{\alpha} = e^{-\left(\frac{E_F}{kT}\right)}$ of FD gas. Now, depending on this temperature how would you classify the degenerate state of FD gas? (whether it is very weakly degenerate, weakly degenerate or strongly degenerate?)
 - (b) Show that the number of Fermions per unit volume of a strongly degenerate FD gas is

$$n = \left(\frac{8\pi}{3}\right) \left(\frac{2m}{\hbar^2}\right)^{\frac{3}{2}} F_{F_0}^{\frac{3}{2}}.$$

(c) What is Fermi temperature? Show that the degeneracy parameter $p_0 = \frac{2}{5}nk_BT_F$, where *n* is the number of molecules per unit volume and T_F is the Fermi temperature. (2+4)+1+3